

A PYTHON PACKAGE FOR MODELLING THE PHOTOMETRIC SIGNATURES OF EXOPLANETARY RINGS/SATELLITES

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pryngles-public

PlanetaRY spanGLES



Solar, Earth & Planetary Physics



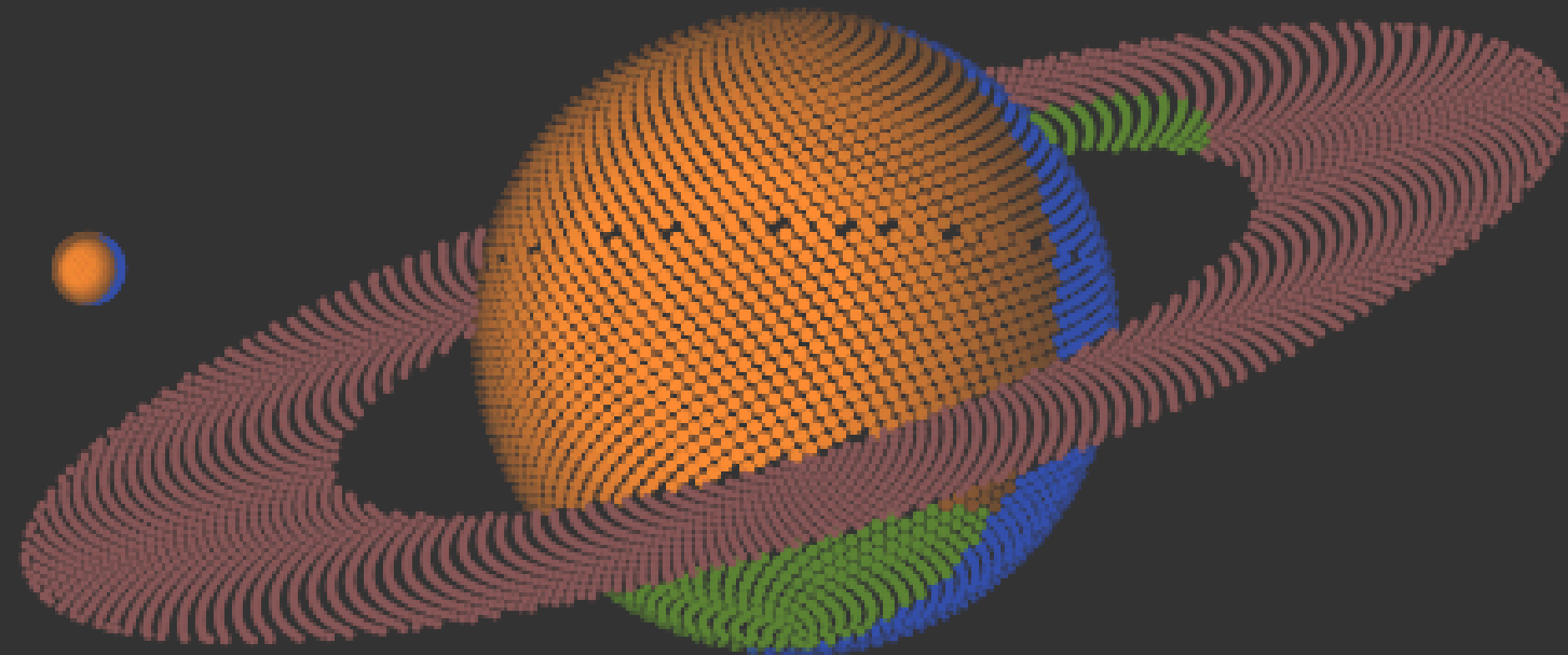
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Grupo de
Física y Astrofísica
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PRYNGLES 0.9.10 (C) 2022
[HTTPS://GITHUB.COM/SEAP-UDEA/PRYNGLES-PUBLIC](https://github.com/seap-udea/pryngles-public)

JORGE I. ZULUAGA, MARIO SUCERQUIA & JAIME A. ALVARADO-MONTES
WITH CONTRIBUTIONS OF ALLARD VEENSTRA

ANILLOS/SATÉLITES EXOPLANETARIOS ¿DÓNDE ESTÁN?

→ PRESENCIA TÍPICA DENTRO DEL SISTEMA SOLAR

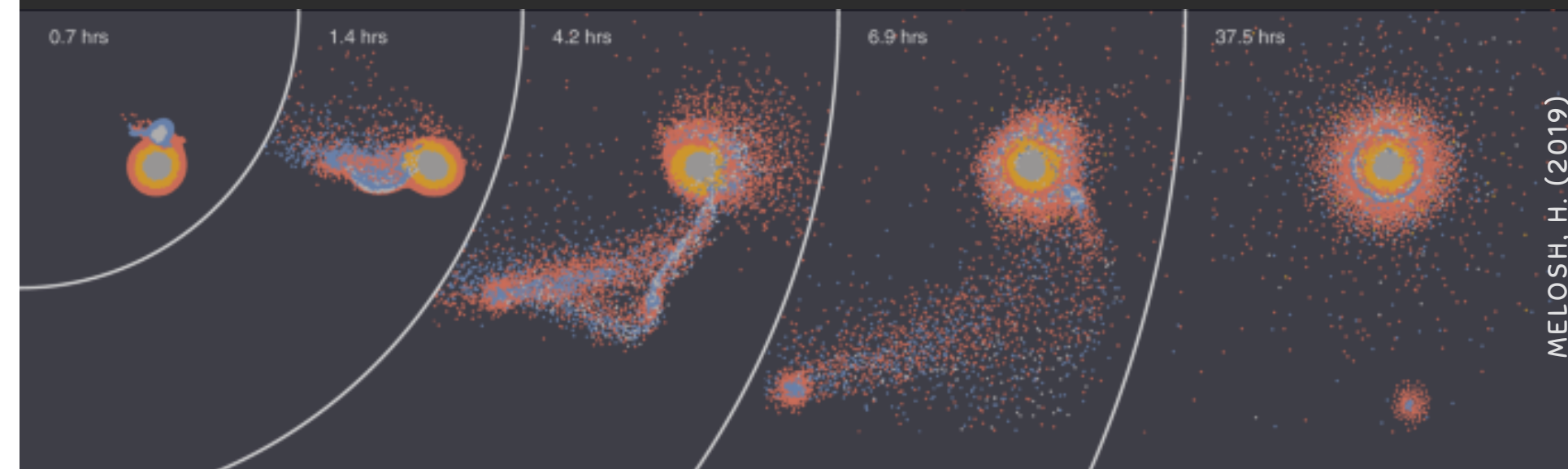
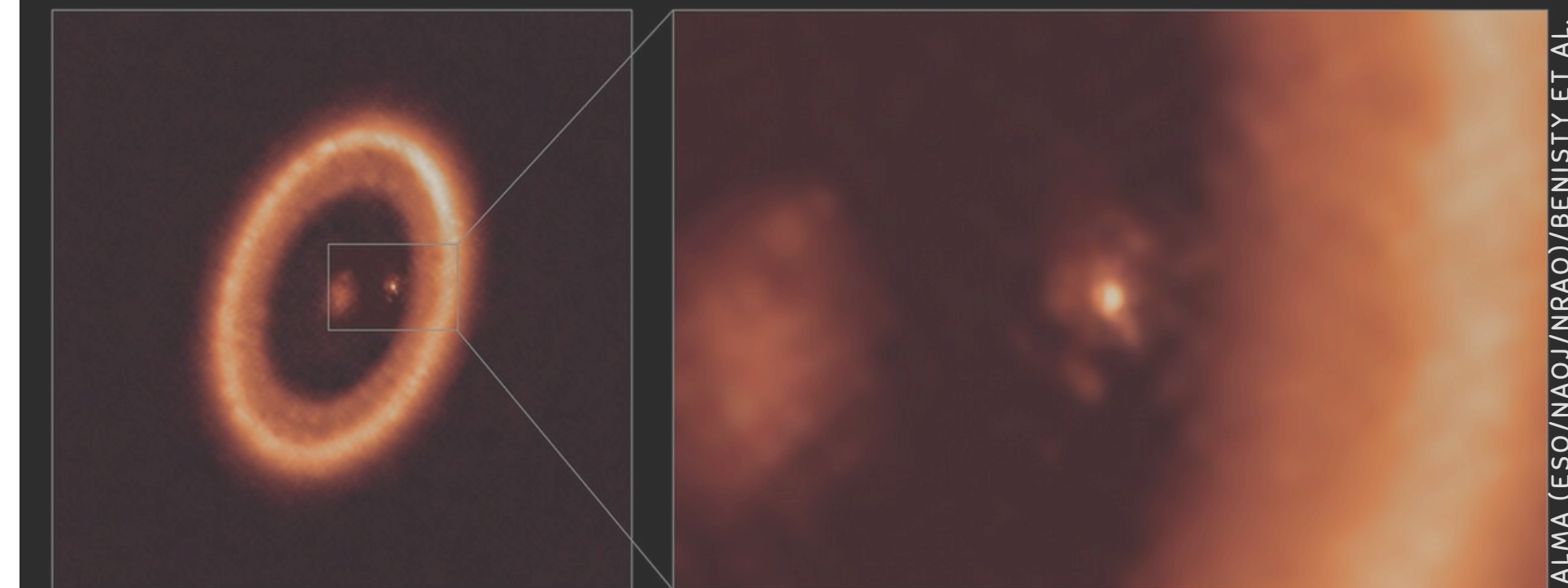
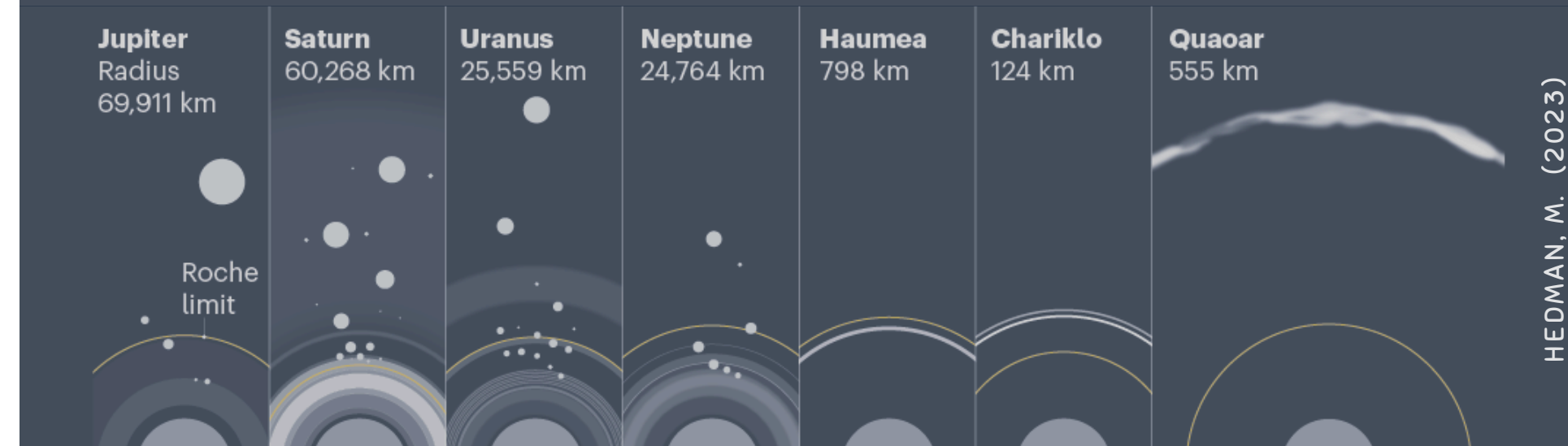
RESULTADO DE:

- FORMACIÓN Y EVOLUCIÓN PLANETARIA
PDS 70c - A. ISELLA, ET AL. 2019
- IMPACTOS Y COLISIONES
ORIGIN OF THE MOON - R. CANUP, 2012
- DISRUPCIONES DE MAREA
SATURN'S RINGS - J. WISDOM, ET AL. 2022

→ ¿QUÉ TAN COMUNES Y ABUNDANTES SON ESTAS ESTRUCTURAS?

→ ¿SON ESTRUCTURAS ESTABLES O TRANSITORIAS?

→ ¿CUÁLES SON SUS CARACTERÍSTICAS Y DIVERSIDAD?



ANILLOS/SATÉLITES EXOPLANETARIOS ¿DONDE ESTÁN?

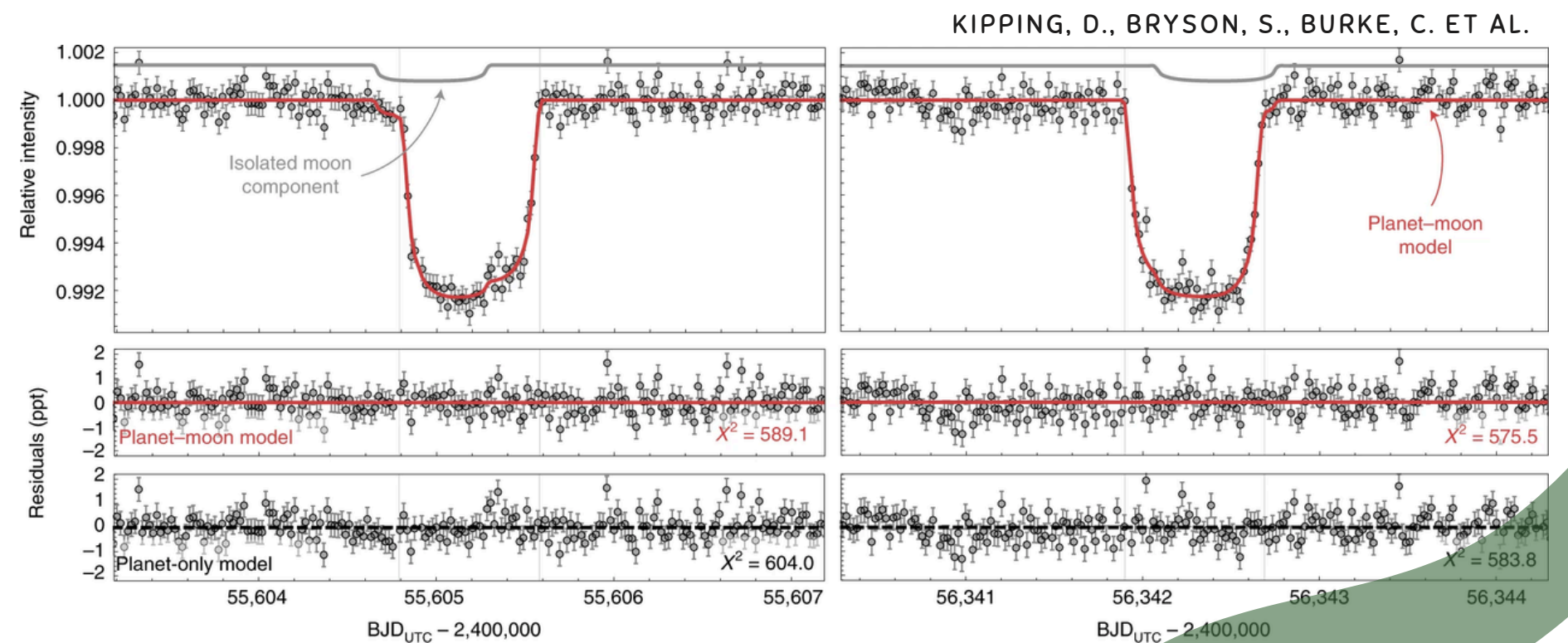
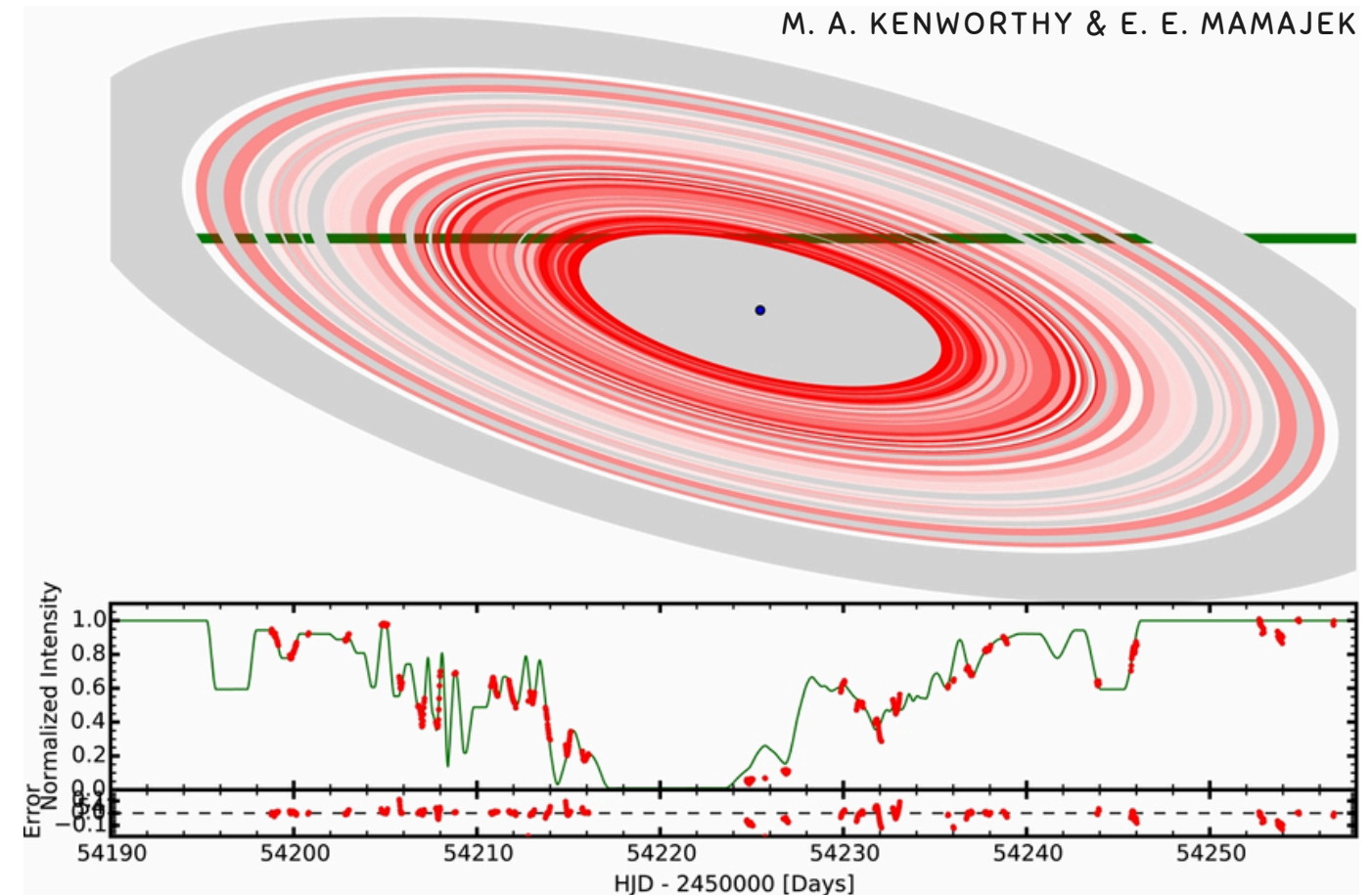
¿SEÑALES DÉBILES PARA DISCERNIR DEL RUIDO?
→ R. HELLER. 2018

SUB-MERCURY EXOPLANET KEPLER 37b
→ T. BARCLAY, ET AL. 2023

LUZ REFLEJADA POR ANILLOS KRONIANOS -10^2 ppm
→ J. I. ZULUAGA, ET AL. 2020

POSIBLES CANDIDATOS:

- EXORING - J1407 B
(M. A. KENWORTHY & E. E. MAMAJEK. 2015)
- EXOMOON - KEPLER 1708 B
(KIPPING, D., BRYSON, S., BURKE, C. ET AL. 2022)



PRYNGLS¹

DISCRETIZANDO SUPERFICIES...

→ [HTTPS://GITHUB.COM/SEAP-UDEA/PRYNGLS-PUBLIC](https://github.com/SEAP-UDEA/PRYNGLS-PUBLIC)   python™

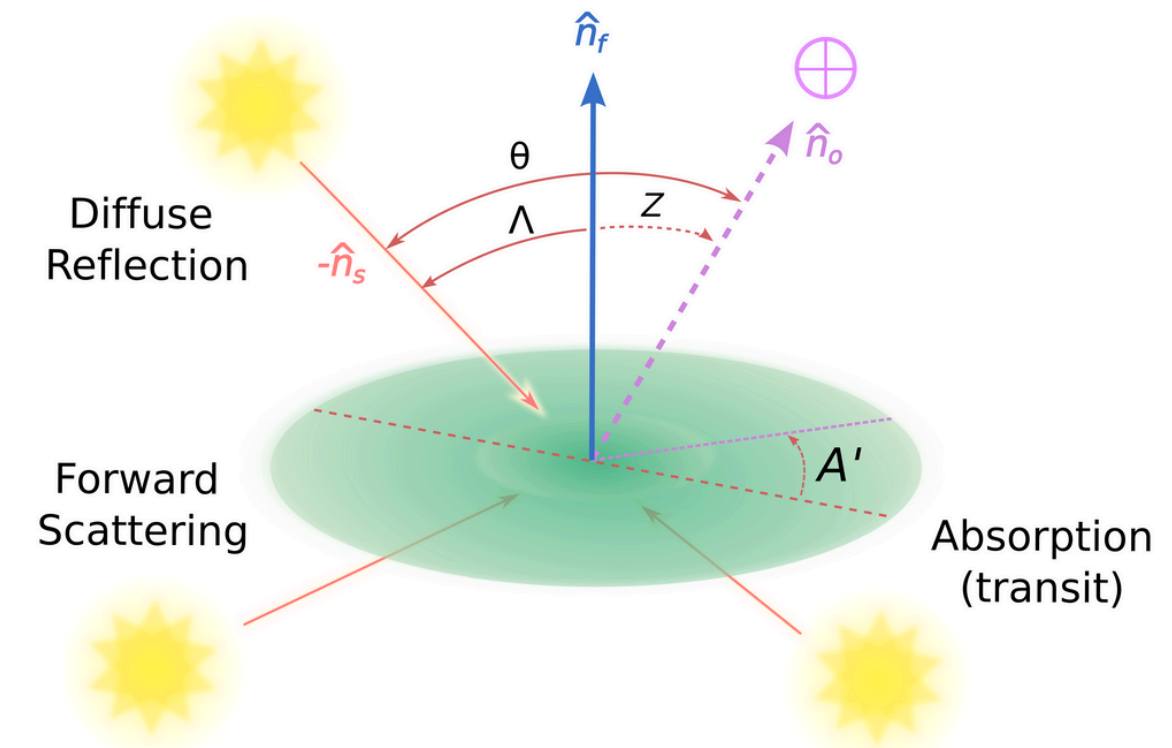
→ ¹J. I. ZULUAGA, M. SUCERQUIA & J. A. ALVARADO-MONTES
WITH CONTRIBUTIONS OF A. VEENSTRA

ATRIBUTOS DE SPANGLES:

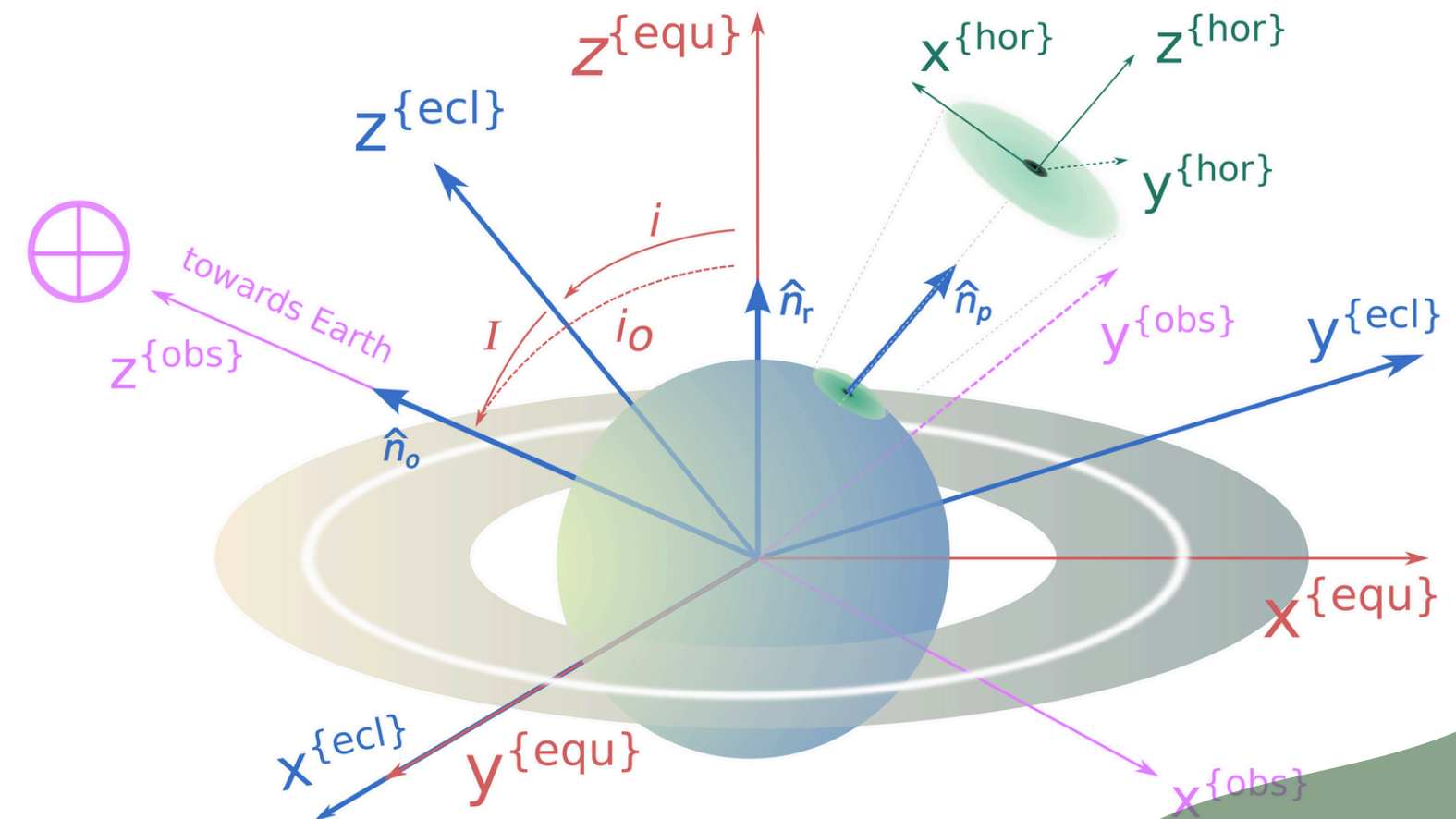
1. ESTADOS
(ILUMINADO, VISIBLE, OCULTO, TRÁNSITO, ETC.)
2. COORDENADAS
(FUENTE, OBSERVADOR, EQU, ECL, ALT-AZ, ETC.)
3. PARÁMETROS FÍSICOS
(ALBEDO, OPACIDAD, EMISIVIDAD, ETC.)

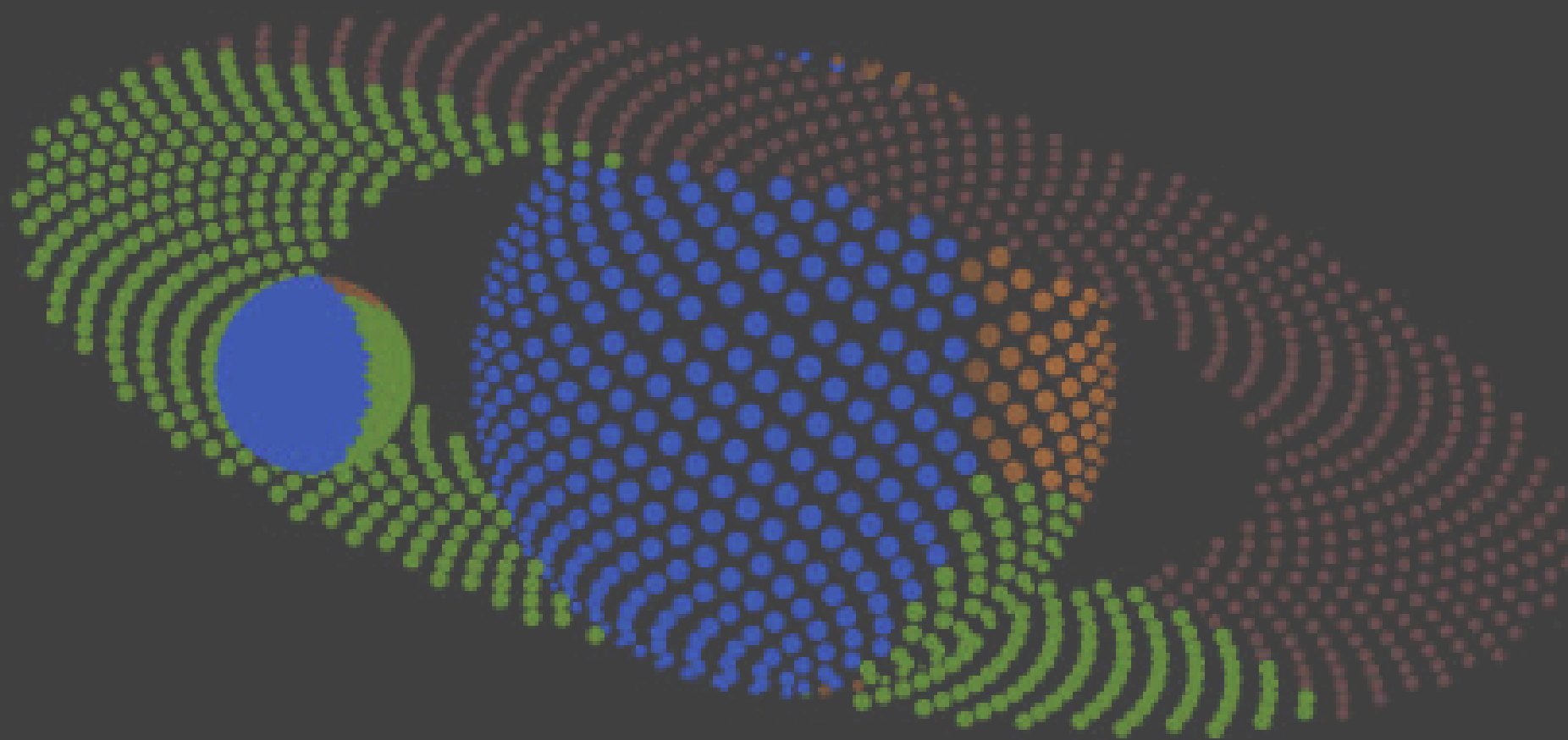
MODELAMIENTO DE EFECTOS ÓPTICOS:

- TRÁNSITO
- SCATTERING
- POLARIZACIÓN (ADAPTADO DE *PyMieDAP*)



ZULUAGA J. I; SUCERQUIA M & ALVARADO-MONTES J. A.





Scattered light may reveal the existence of ringed exoplanets

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The bright side of the light curve: a general photometric model of non-transiting exorings

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ARTICLE INFO

Keywords:

planets and satellites: rings

techniques: photometric

methods: numerical

planets and satellites: detection

ABSTRACT

Rings around exoplanets (exorings) are one of the most expected discoveries in exoplanetary research. There is an increasing number of theoretical and observational efforts for detecting exorings, but none of them have succeeded yet. Most of those methods focus on the photometric signatures of exorings during transits, whereas less attention has been paid to light diffusely reflected: what we denote here as the bright side of the light curve. This is particularly important when we cannot detect the typical stellar flux drop produced by transiting exoplanets. Here, we endeavour to develop a general method to model the variations on the light curves of both ringed non-transiting and transiting exoplanets. Our model (dubbed as *Pryngles*) simulates the complex interaction of luminous, opaque, and semitransparent objects in planetary systems, discretizing their surface with small circular plane discs that resemble sequins or spangles. We perform several numerical experiments with this model, and show its incredible potential to describe the light curve of complex systems under various orbital, planetary, and observational configurations of planets, moons, rings, or discs. As our model uses a very general approach, we can capture effects like shadows or planetary/ring shine, and since the model is also modular we can easily integrate arbitrarily complex physics of planetary light scattering. A comparison against existing tools and analytical models of reflected light reveals that our model, despite its novel features, reliably reproduces light curves under common circumstances. *Pryngles* source code is written in Python and made publicly available.

A general polarimetric model for transiting and non-transiting ringed exoplanets

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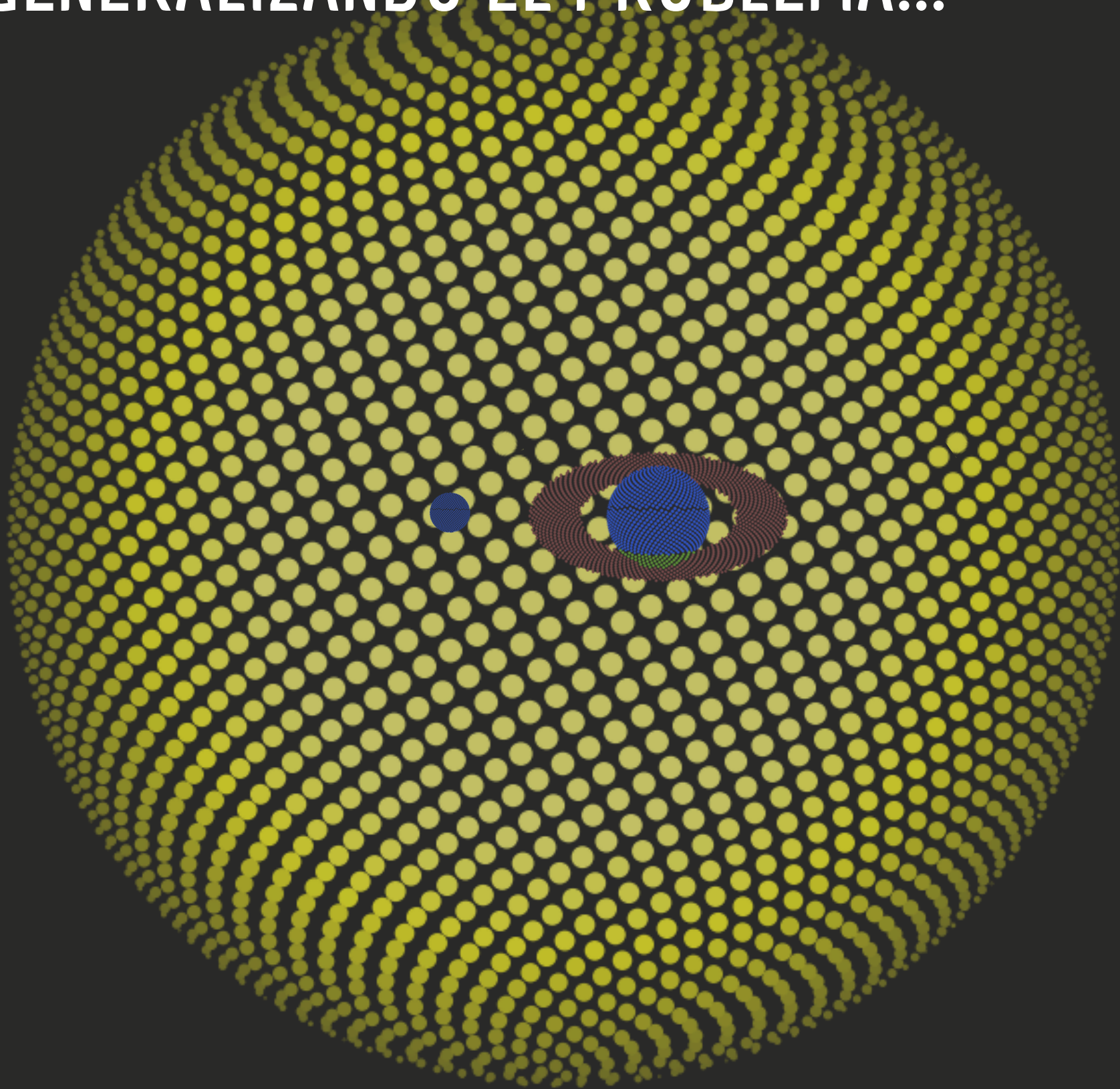
⁵ Instituto de Física y Astronomía, Facultad de Ciencias, Universidad de Valparaíso, Av. Gran Bretaña 1111, 5030 Casilla, Valparaíso, Chile

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PRYNGLS GENERALIZANDO EL PROBLEMA...



INTERFAZ *RingedPlanet* (2022):

1. SISTEMAS ESTRELLA-PLANETA-ANILLO
2. MARCO DE REFERENCIA PLANETOCÉNTRICO,
3. DINÁMICA ANALÍTICA → PROBLEMA DE KEPLER

→ EFECTOS TESTEADOS $\varepsilon \lesssim 10^{-4}$:

1. PAQUETES EXTERNOS → *batman & PyPplusS*
2. MODELOS ANALÍTICOS → M. SUCERQUIA, ET AL. 2020

INTERFAZ *System* (DEV):

1. SISTEMAS ARBITRARIOS
2. MARCO DE REFERENCIA BARICÉNTRICO
3. INTEGRACIÓN NUMÉRICA → REBOUND
4. REESTRUCTURACIÓN DE ARQUITECTURA MODULAR
5. GESTIÓN CENTRALIZADA DE SPANGLES → PANDAS

→ EFECTOS TESTEADOS $\varepsilon \lesssim 10^{-5}$:

1. INTERFAZ *RingedPlanet*
2. PROXIMAMENTE PAQUETES EXTERNOS
→ *Pandora, LUNA, Gefera*

PRYNGLES MODELANDO FOTOMETRÍA...

REFLEXIÓN DIFUSA $\rightarrow \frac{F}{F_0} = \sum_i \frac{a_{S_i} \cos \Lambda_i}{4\pi d_i^2} A_{L_i}(\Lambda_i) \cos Z_i$

ATMOSFERAS \rightarrow (SOBOLEV V.V. 1975)

$A_{L_i}(\Lambda_i) = 2 \int_0^1 \cos Z \rho(\gamma, \Lambda_i, Z) d(\cos Z) \rightarrow$ ALBEDO LAMBERTIANO

1. SEMI-INFINITA $\tau \rightarrow \infty$
2. ISOTRÓPICAMENTE GRIS

$\rho(\gamma, \Lambda, Z) = \frac{\gamma f(\gamma, Z) f(\gamma, \Lambda)}{4 \cos \Lambda + \cos Z} \rightarrow$ COEFICIENTE DE REFLEXIÓN

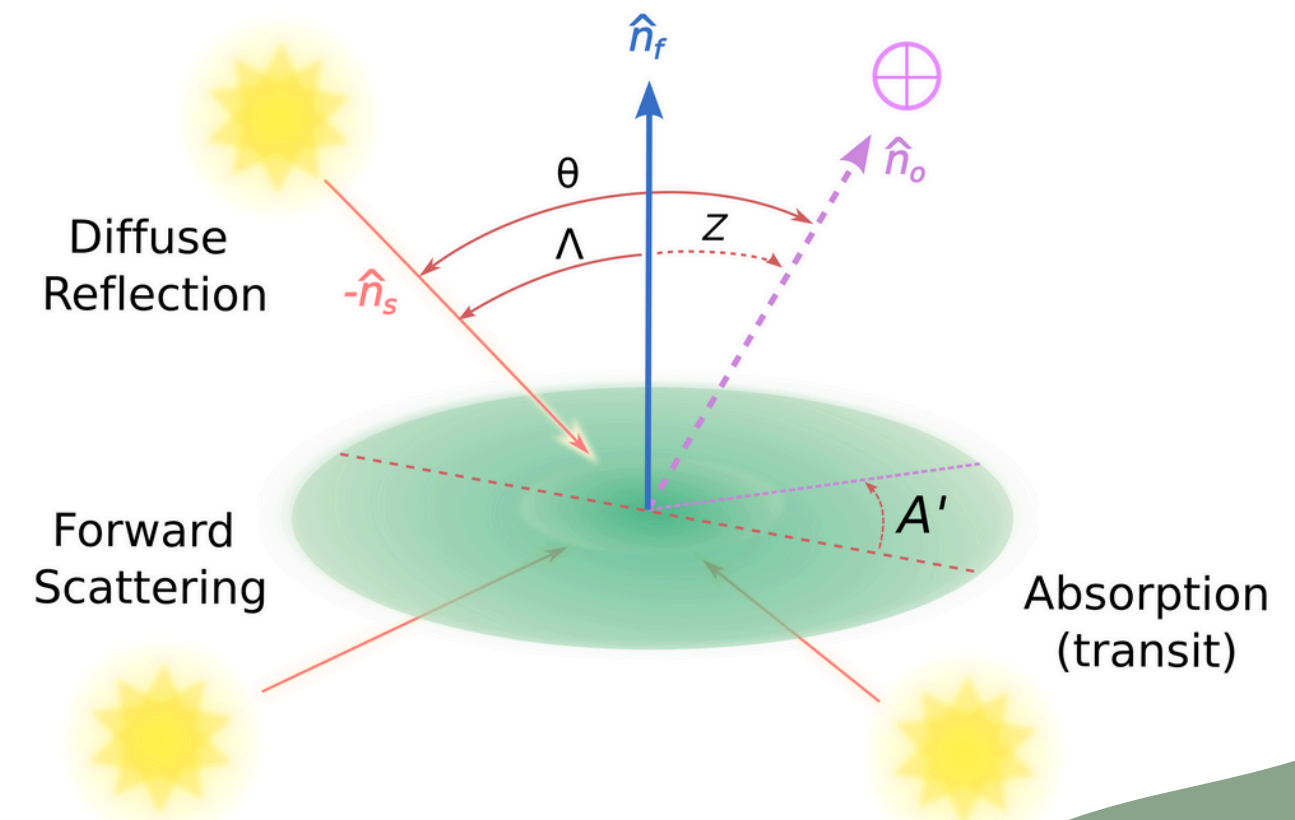
$A_S = 4 \int_0^1 \int_0^1 \cos \Lambda \cos Z \rho(\gamma, \Lambda, Z) d(\cos \Lambda) d(\cos Z) \rightarrow$ ALBEDO ESFÉRICO

SUPERFICIES \rightarrow (RUSSEL H. N. 1916):

$A_{L_i}(\Lambda_i) = 2\pi\gamma \int_0^1 \frac{f(\Lambda_i, Z)}{\cos \Lambda} d(\cos Z) \rightarrow$ ALBEDO LAMBERTIANO

LEY DE REFLEXIÓN DIFUSA:

1. LEY DE LAMBERT
2. LEY DE LOMMEL-SEELIGER $\rightarrow f(\Lambda, Z) = \begin{cases} \cos \Lambda \\ \frac{\cos \Lambda \cos Z}{\cos \Lambda + \cos Z} \end{cases}$



ZULUAGA J. I; SUCERQUIA M & ALVARADO-MONTES J. A.

PRYNGLES ESTRUCTURAS DETECTABLES...

CORRELACIÓN DE MAGNITUDES FOTOMÉTRICAS:

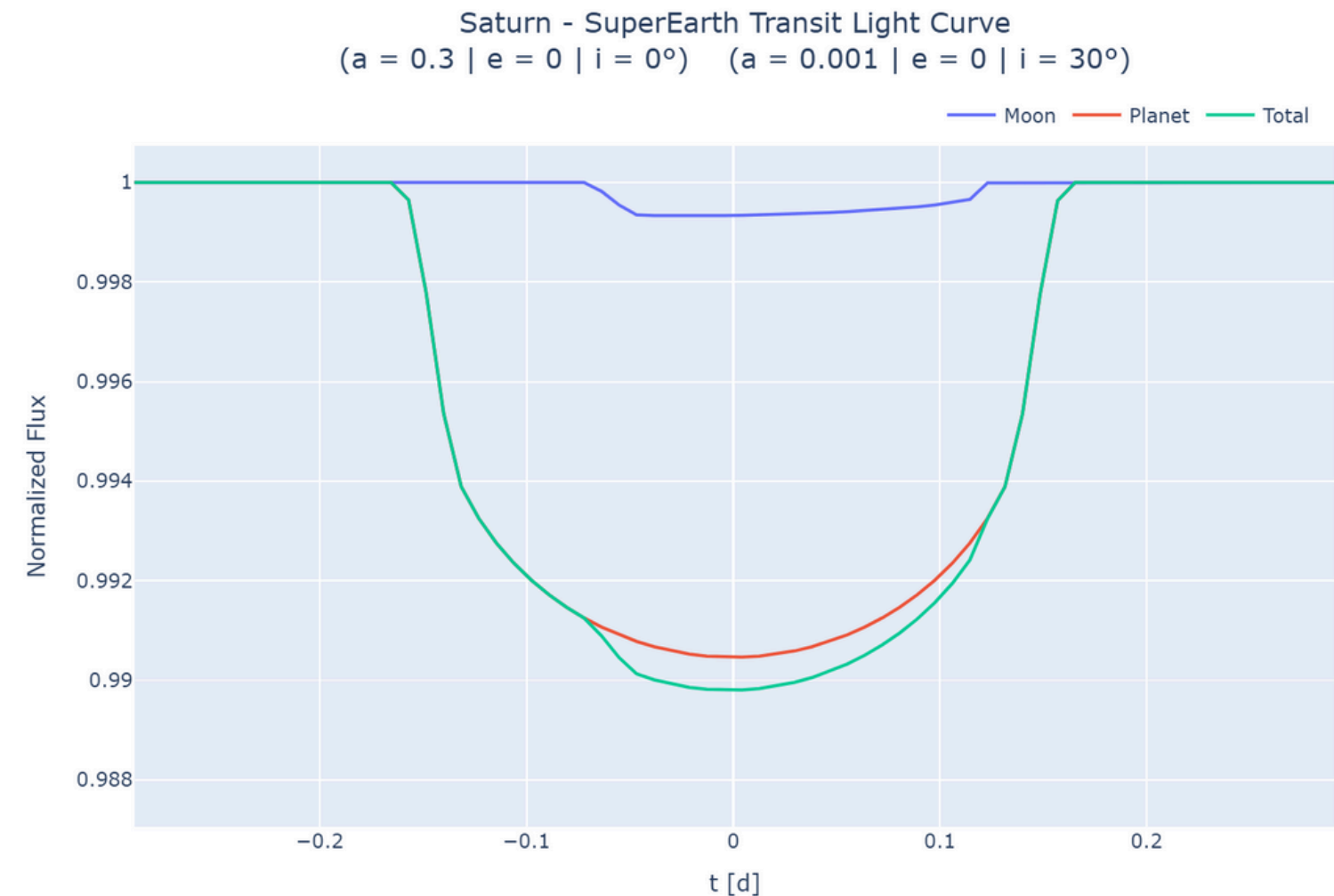
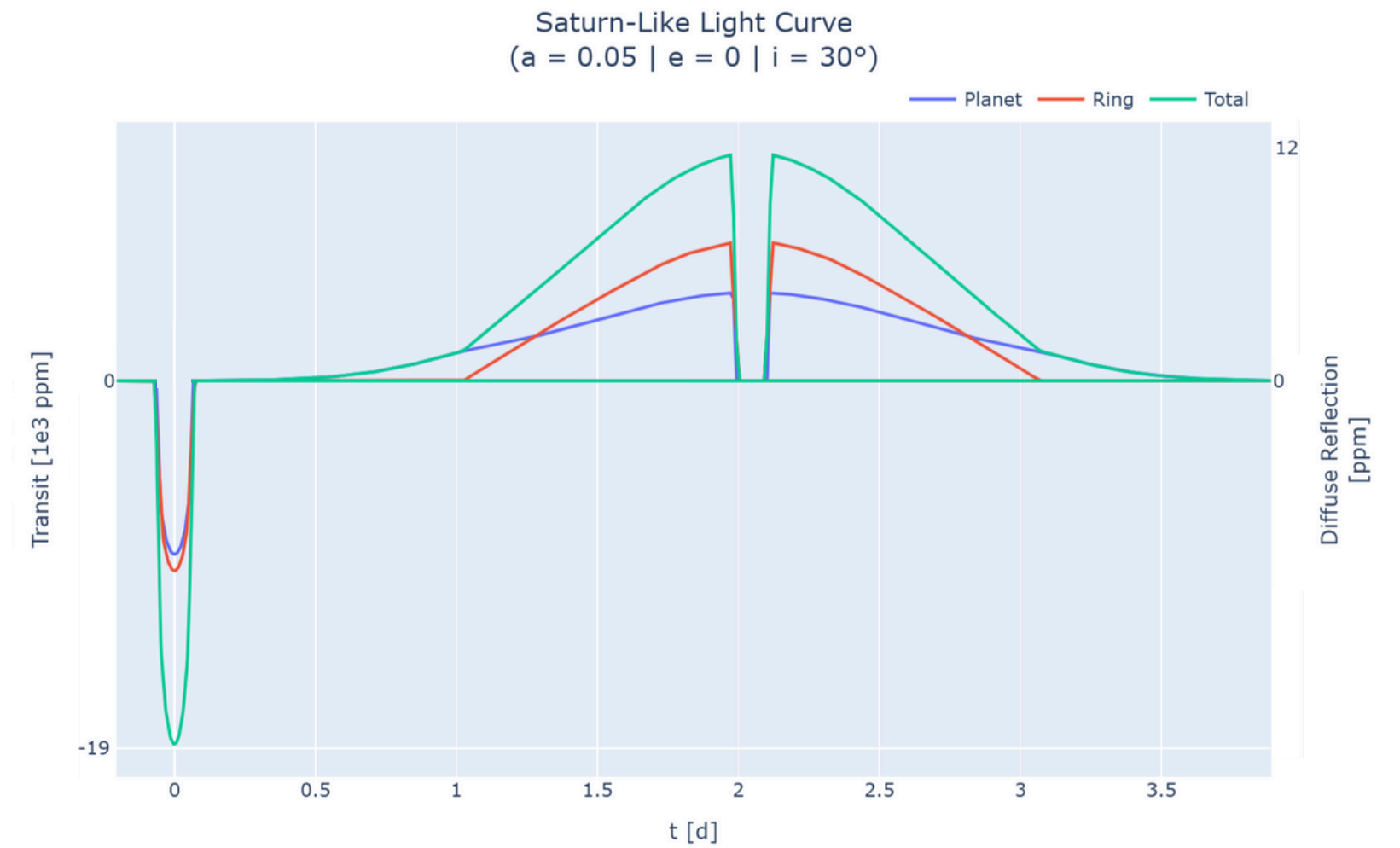
1. TAMAÑO DEL CUERPO
2. DISTANCIA A LA ESTRELLA
3. NATURALEZA DE LA ÓRBITA
4. ORIENTACIÓN DE LINEA DE VISIÓN

TRÁNSITO:

- SUBESTIMACIÓN DE DENSIDADES
- RESOLUCIÓN DE OBJETOS ADICIONALES
- ANÁLISIS DE VARIACIONES DE TRÁNSITO

REFLEXIÓN DIFUSA:

- TRAZAS OBSERVABLES EN TRÁNSITO PRIMARIO/SECUNDARIO



PRYNGLES ESTRUCTURAS DETECTABLES...

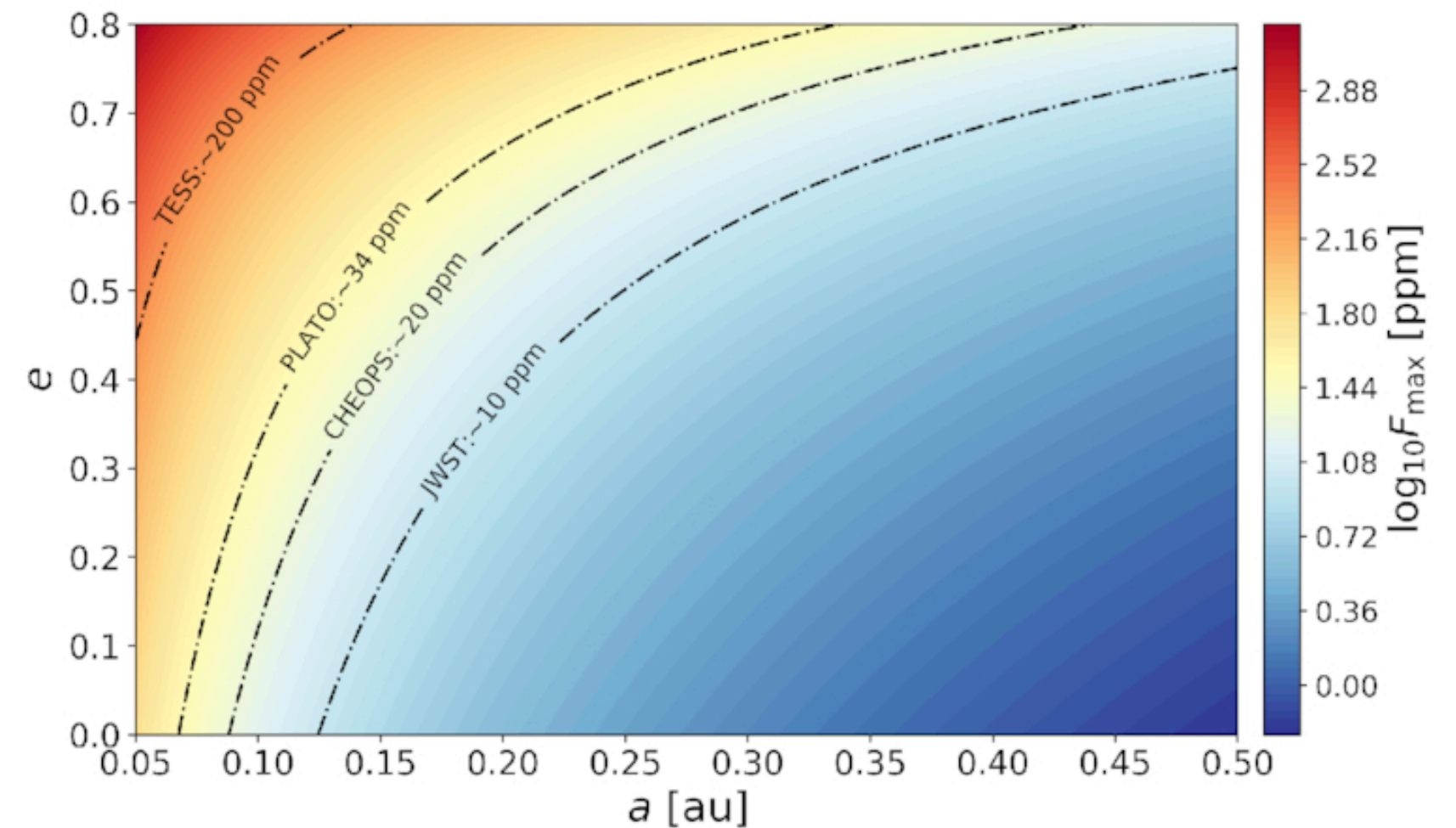
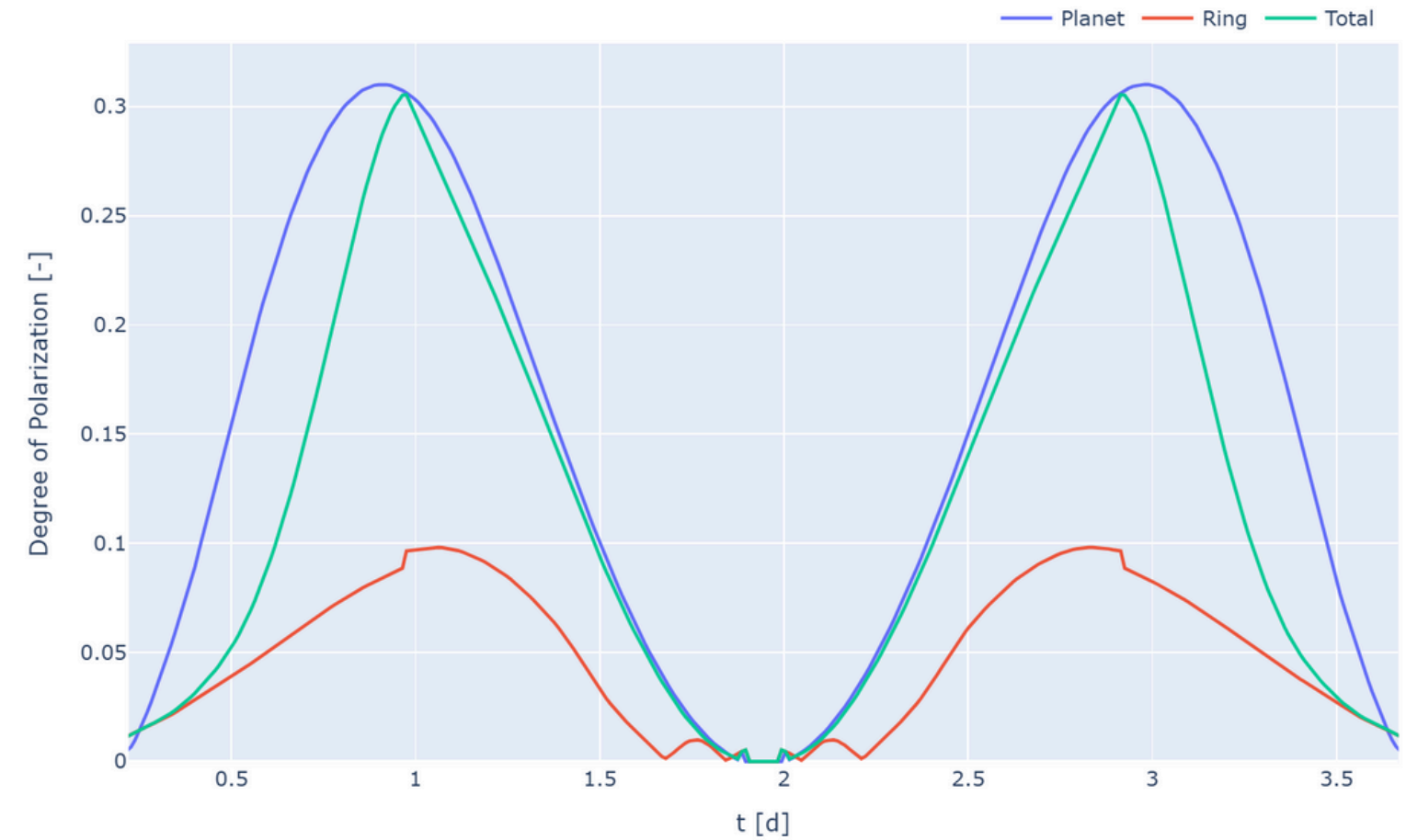
CAPACIDAD OBSERVACIONAL:

1. ESPACIO DE PARÁMETROS RESTRINGIDO
2. LIMITACIÓN EN TIEMPOS DE OBSERVACIÓN
3. MENOR VARIEDAD DE SISTEMAS RESOLUBLES
4. PRECISIÓN INSTRUMENTAL REQUERIDA Y FUTURA

SCATTERING:

- REDUCCIÓN EN EL GRADO DE POLARIZACIÓN
- TRAZAS OBSERVABLES EN TRÁNSITO PRIMARIO

Saturn-Like Light Curve
($a = 0.05$ | $e = 0$ | $i = 30^\circ$)



PRYNGLES UN FUTURO PROMETEDOR...

→ REVISIÓN, REPRODUCCIÓN Y MOTIVACIÓN DE OBSERVACIONES

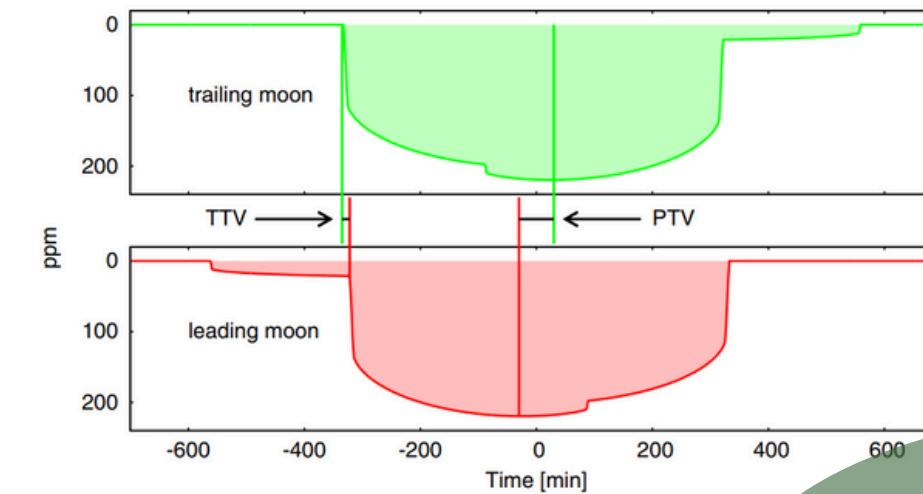
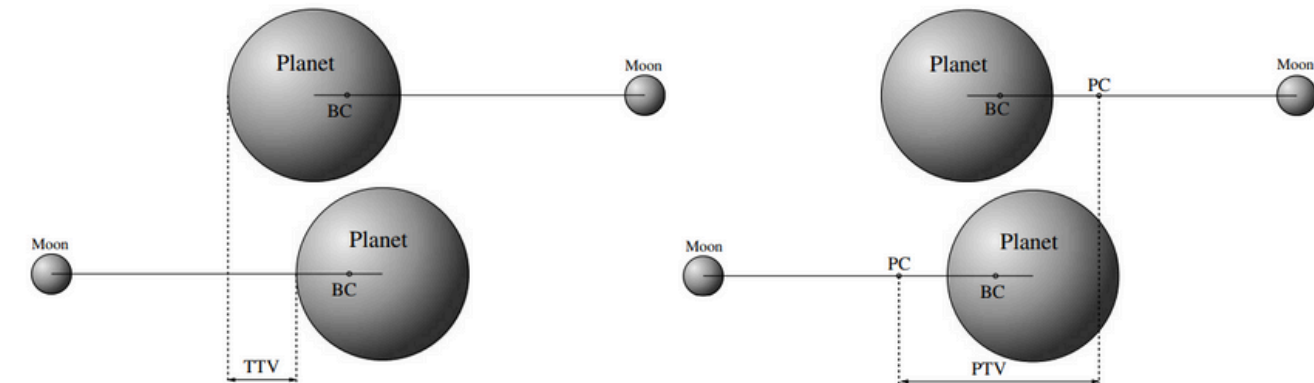
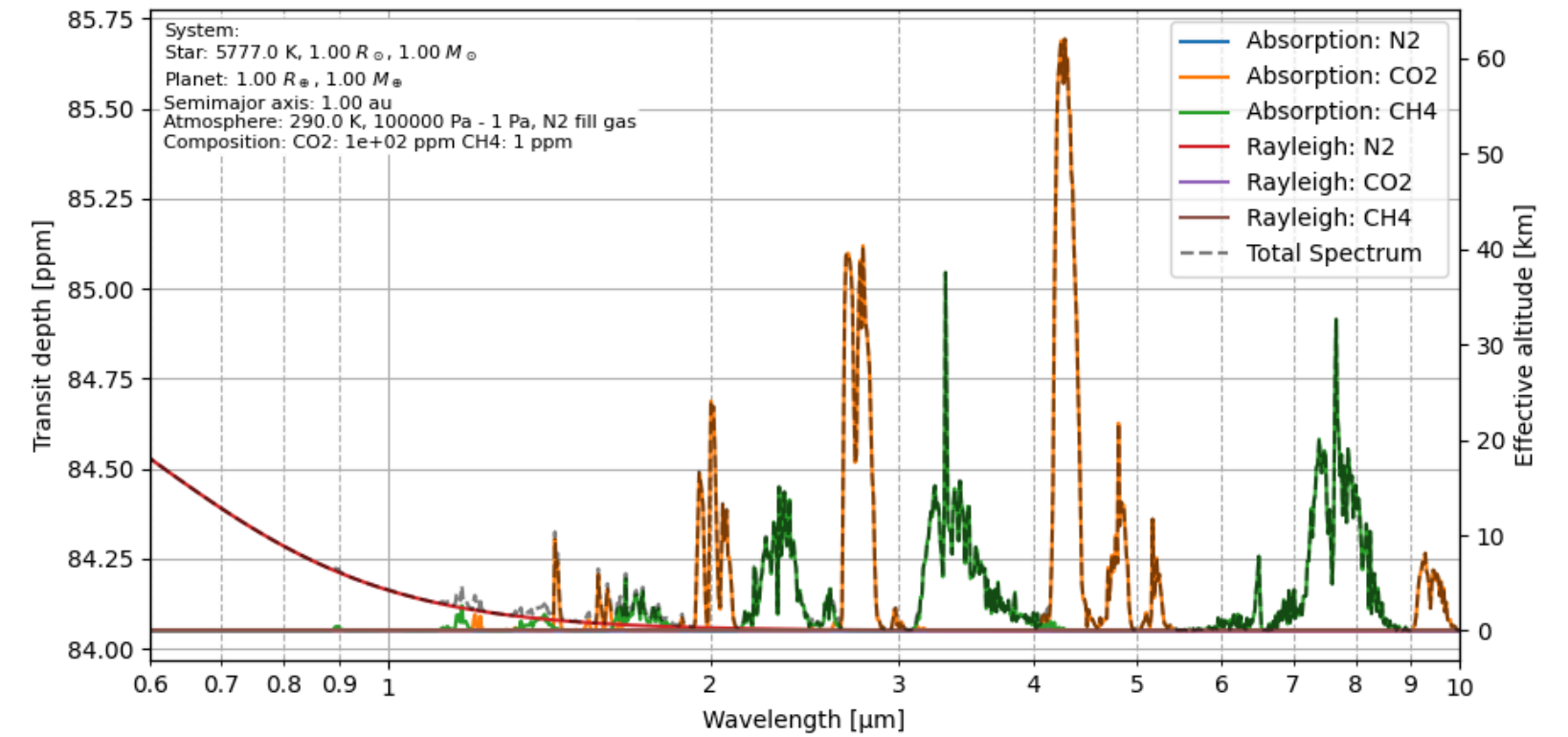
PROSPECTOS:

1. TÉCNICAS DE TTV/TDV
2. MAPEO DE SUPERFICIES/ATMOSFERAS
3. ANÁLISIS DE DIVERSIDAD Y ESTABILIDAD
4. IMPLEMENTACIÓN DE MODELOS MULTIBANDA
5. AJUSTES A MODELOS DE COMPOSICIÓN Y DINÁMICA INTERNA

OTRAS APLICACIONES:

→ ASTROFÍSICA ESTELAR (BINARIAS ECLIPSANTES)

D. S. DUQUE-CASTAÑO, J. I. ZULUAGA & L. FLOR-TORRES. 2024



R. HELLER. 2018



**NOS MANTENEMOS EXPECTANTES DE LA PRIMER DETECCIÓN EN
ANILLOS Y SATÉLITES EXOPLANETARIOS**

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